Fully Coupled 1-D Mobile Bed River Sediment Transport Model

(Unsteady Flow and Non-equilibrium Sediment Transport with Looped Network System)

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Objective

Create a fully coupled 1-dimensional erodible bed with suspended and bed load sediment transport model with looped network system

Conditions:

- Unsteady flow
- Separate sediment transport by Bed load and Suspended load
- Non-equilibrium sediment transport
- Looped network system
- Trap efficiency (deposit and transported)

Model application:

- Belley area (18 km:11.3 miles) of upper Rhone River in France
- France National Rhone River Authority (CNR)

Location



Location – Southwest of France



Downstream of Rhone River- Marseille



Rhone River & Arve River



Practical Aspects of Computational River Hydraulics

J.A. Cunge, F.M. Holly, Jr

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International Institute for Hydraulic and Environmental Engineering, Delft

R Pitman Advanced Publishing Program Boston · London · Melbourne 136 Practical Aspects of Computational River Hydraulics



Fig. 4.2. Present and proposed development on the Rhône River in France

Rhone River (Geneva-Lyon)



Upper Rhone Management



Belley area management

 Every 3 years of flushing event at upstream reservoirs (Verbois & Chancy-Pougny in Swiss and Genissiat, Seyssel & Chautagne in France)

Concerns:

- Quantity of sediment deposit in Belley Reservoir
- Suspended load for downstream nuclear power plant water intake facility near Lyon
- Need flushing operation at Belley Reservoir

Fluvial Sediment

- Process of erosion, transport and deposition very complex
- Entrainment and transportation solid particle & fluid movement
- Solid particle density, shape, size & status of surface
- Fluid movement flow type, velocity & viscosity
- Predict a condition of equilibrium or erosiondeposition
- Determine the quantity transported by the river

Various Issues of Sediment Deposit

- Impact the carrying capacity (Conveyance) of river/channel
- Reduce the flood control capability
- Increase the damage by flooding
- Increase of maintenance/ management cost
- Reduce the original objective of structure

Hydraulics & Geometry

Hydraulics

- Governing equation
- Steady flow, Unsteady flow
- Subcritical, Supercritical
- Roughness coefficient: n value
- Energy coefficient / Momentum coefficient
- Branched network & looped network
 - Divergence
 - Confluence
 - Looped

Hydraulics & Sediment Transport Model

- Define the objective (purpose) of project
- Decide how and where to apply the model
- Boundary condition
 - Upstream & Downstream
- Bed Load, Suspended Load & Total Load
- Model coupling
 - Uncoupled model & Fully coupled model
- Roughness coefficient with bed form
 - Ripple, Dune & Anti-dune
- Scheme
 - Explicit & Implicit
- Selection of sediment transport formulas
- Application for real natural river

Bed Form



Figure 1-1. Bedform types under increasing Froude number (A to H) [Van Rijn, 1993; adopted from Simons and Richardson, 1966].

Bed Form Example



Ripples in Bed of Fine Sand in Flume 10.5 in. Wide; Hwang (1965) (Flow was to Left; Flow Depth = 0.241 ft, Mean Velocity = 1.25 fps, $d_{so} = 0.230$ mm, $\sigma_s = 1.43$)



Antidunes in Flume 10.5 in. Wide; Kennedy (1960) (Flow was to Left; Scale in Figure is in inches; Mean Flow Depth = 0.248 ft, Mean Velocity = 3.30 tps, Froude Number = 1.17, d_{50} = 0.233 mm, σ_{g} = 1.47)



Configuration of a Gravel Dune



Bedload samples corresponding to the dashed lines are shown below. The vertical scale bars are 10 centimeters or 4 inches long.



Research/ Study Process

Selection of Sediment Transport Formulas Cross Section Data Drive Partial Differential Equation Create Numerical Model - Nonequilibrium Sediment Transport Test and Verification

Selection of Sediment Transport Formulas

- Many formulas developed after Duboys (1879)- Laboratory test & Field Measuring
- Application limit: not always clearly mentioned
- Selection of suitable formula:
 - Apply to real natural river condition
 - Difficult to select the proper formula
 - Different formulas give quite different results with the same hydraulic conditions
- Need sensitivity analysis with various hydraulic parameters (Q, V, depth, slope, Froude no.) for equilibrium sediment discharge
- Verification analysis with computer simulation for selected sediment transport formulas

Sediment transport formulas

Author	Dm	Velocity	Remark
Duboys(1879)	0	×	С
Schoklitsch(1935)	++	×	С
Shields(1936)	0	×	С
Meyer—Peter and Muller(1948)	0	×	С
Einstein – Brown (1950)	0	, ×	С
Einstein Bed Load function(1950)	++	0	T, S, C
Laursen(1958)	0	×	т
Shinohara — Tsubaki(1959)	0	×	Т
Garde and Albertson(1961)	0	0	т
Colby(1964)	0	0	т
Engelund—Hansen(1967)	0	0	Т
Inglis—Lacey(1968)	0	0	Т
Toffaleti(1969)	++	0	T, S, C
Ackers – White(1973)	0	0	Т
Yang(1973)	+++-	0	т
Engelund—Fredsoe(1976)	0	0	T, S, C
Holtorff(1983)	++	0	T, S, C
van Rijn(1984)	0	0	T, S, C
Celik and Rodi(1991)	0	0	S
Samaga, Ranga Raju and Garde(1986)	++	0	T, S, C
Rickenmann(1991)	0	0	С

where

- ${\rm O}$: This term exists explicitly in the formula
- imes : This term does not exist explicitly in the formula
- ++ : Serveral Classes of Sediment
- T: Total Load
- C: Bed Load
- S: Suspended Load
- Dm: Reperesentative Diameter



(Fig. 1) Sediment discharge as function of water discharge for Colorado River(after Vanoni, 1977, Sedimentation Engineering)



(Fig. 2) Sediment discharge as function of water discharge for Niobrara River(after Vanoni, 1977, Sedimentation Engineering)

Literature Study of Formula

- □ Shields, Einstein-Brown & Duboys overestimate
- Meyer-Peter Muller underestimate
- Schoklitsch less slope the straight lines of fitted data
- Colby, Toffaleti and Engelund-Hansen best agreement
- Einstein bed load function, Larsen & Inglis-Lacey close to a mean line of data, but not fit the data
- Blench small slope intersecting the data
- Yang, Engelund and Hansen, & Ackers and White better than others in the field and laboratory data
- Bed-load prediction:
 - -Einstein Brown formula seems to be 10 times greater than those predicted by Meyer-Peter Muller and Schoklitsch

Continue

Suspended-load prediction:

- -Toffaleti was best among all the formulas tested
- Total-load Prediction: Yang's (1973) formula seems to be close to the measured suspended load discharge at a higher range of sediment discharge, but much greater at a lower range of sediment discharge
- Yang's (1973) formula very poor results for large-scale river (Flow depth> 1m)
- Engelund-Hansen (E & H), Ackers-White (A & W) and van Rijn were preferable in various cases
- Meyer-Peter Muller (MPM) is also tested because it was commonly used or cited
- van Rijn created four (4) formulas with bed load and suspended load separation

Van Rijn's Bed Load & Suspended Load

- Van Rijn Part I: Bed Load
 - $q_b = 0.053[(s-1)g^{0.5}D_{50}^{1.5}T^{2.1}/D^{*0.3}$
 - or $q_b = C_b V_b \delta_b$
- Van Rijn Part II: Suspended Load
 - $q_s = FVhCa$, Ca=0.015D₅₀/a*T^{1.5}/D*^{0.3}
- □ Van Rijn Part III: Simplified Bed Load
 - $q_b = 0.005 \{ (V-Vcr) / [(s-1)gD_{50}]^{0.5} \}^{2.4} D_{50}^{1.2} V$
- Van Rijn Part III: Simplified Suspended Load q_s=0.012{(V-Vcr)/[(s-1)gD₅₀]^{0.5}}^{2.4}D₅₀D_{*}^{-0.6}Vh^{-0.2} Vcr=0.19D₅₀^{0.1}log(12R/3D₉₀) for 100<D₅₀<500µm Vcr=8.5D₅₀^{0.6}log(12R/3D₉₀) for 500<D₅₀<2000µm</p>

Reference Level and Conenctration



(Fig. 3) Definition sketch for reference level and reference concentration

Predicting Entrainment of Sediment into Suspension

(Table. 2) Performance of various formula

Formula	Me	Ad	
Einstein(1950)	1.37	3.45	
Engelund and Fredsoe(1976)	0.50	5.3	
Smith and McLean(1977)	0.88	2.42	
Itakura and Kish(1980)	6.70	2.22	
van Rijn(1984)	1.31	2.19	
Celik and Rodi(1984)	2.57	2.03	
Akiyama and Fukushima(1986)	0.12	8.15	
Proposed formulation	1.00	2.12	

Where

Me : mean value of discrepancy ratio Caep/ Caeo

Ad : mean absolute deviation of discrepancy ratio Caep/ Caeo

Caeo, Caep : observed and predicted values of equilibrium near-bed sediement concentration



Oliver
Oliver
Mc Nown and Lin
Richardson and Zaki

 X Test of Mc Nown and Lin(measured)
Test of Oliver (measured)

(Fig. 4) Comparison of the fall velocity formulas with measured data

Test Selected Sediment Transport Formulas

Selected 7 transport formulas were tested

- Engelund-Hansen (E & H)
- Ackers-White (A & W)
- Meyer-Peter Muller (MPM)
- van Rijn: 4 formulas
- Test diameter of sediment between 0.005 mm(5 µm: very fine silt) and 100 mm (10 cm: small cobbles)
- Analyze the sensibility of the formulas
- Various hydraulic parameters (discharge, energy line, velocity, depth, width and Froude number)

Hydraulic Parameters

(Table. 3) Hydraulic parameters used by computer simulation

Depth h(m)	Width B(m)	Area A(m³)	n (Kst)	Hydraulic Radius R(m)	Ι.	Velocity V(m/s)	Discharge Q(m²/s)	Froude number Fr	Remark
0.2	1.0	0.2	0.014 (72)	0.14	1/ 500 - 1/ 750 0	0.88~0.23	0.17~0.05	0.62~0.16	Test 11~15
0.8	5.0	4.0	0.018 (56)	0.61	1/ 500- 1/ 7500	1.78~0.46	7.12~1.84	0.64~0.16	Test 21~25
1.0	10	10	0.020 (50)	0.83	1/ 500- 1/ 10000	1.98~0.44	19.8~4.44	0.63~0.14	Test 31~36
1.5	30	40	0.022 (46)	1.36	1/ 2500 - 1/ 12000	1.12~0.51	50.3~23.0	0.29~0.13	Test 41~45
4.5	200	900	0 .03 1 (32)	4.31	1/ 2500- 1/ 12000	1.71~0.78	1537~701	0.26~0.12	Test 51~55
10.0	300	3000	0.035 (29)	9.38	1/ 2500- 1/ 20000	2.54~0.90	7622~2695	0.26~0.09	Test 61~66

where

n : Manning roughness coefficient

I : Slope of energy grade line

Kst : Strickler coefficient

Test No.	Depth h(m)	Width B(m)	Area A(m')	n	I	Velocity V(m/s)	Discharge Q(m²/s)	Froude number Fr
11 12 13 14 15	0.2	1.0	0.2	0.014	1/ 500 1/ 1000 1/ 2500 1/ 5000 1/ 7500	0.87 0.62 0.39 0.28 0.23	0.175 0.123 0.078 0.055 0.045	0.62 0.44 0.28 0.20 0.16
21 22 23 24 25	0.8	5.0	4.0	0.018	1/ 500 1/ 1000 1/ 2500 1/ 5000 1/ 7500	1.78 1.26 0.80 0.56 0.46	7.12 5.03 3.18 2.25 1.84	0.64 0.45 0.28 0.20 0.16
31 32 33 34 35 36	1.0	10.0	10.0	0.020	1/ 500 1/ 1000 1/ 2500 1/ 5000 1/ 7500	1.98 1.40 0.89 0.63 0.51 0.44	19.80 14.00 8.85 6.26 5.10 4.44	0.63 0.45 0.28 0.20 0.16 0.14
41 42 43 44 45	1.5	30.0	45.0	0.022	1/ 2500 1/ 5000 1/ 7500 1/ 10000 1/ 12000	1.12 0.79 0.64 0.56 0.51	50.31 35.57 29.00 25.12 22.94	0.29 0.21 0.17 0.15 0.13
51 52 53 54 55	4.5	200.0	900.0	0.031	1/ 2500 1/ 5000 1/ 7500 1/ 10000 1/ 12000	1.71 1.21 0.99 0.85 0.78	1537.0 1087.0 886.0 768.0 701.0	0.26 0.18 0.15 0.13 0.12
61 62 63 64 65 66	10.0	300.0	3000.0	0.035	1/ 2500 1/ 5000 1/ 7500 1/ 10000 1/ 12000 1/ 2000	2.54 0.80 1.47 1.27 1.16 0.90	7622.0 5389.0 4394.0 3811.0 3479.0 2695.0	0.26 0.18 0.15 0.13 0.12 0.09

⟨Table. 4⟩ Hydraulic parameters for Test 11-66














MPM formula

- Increase abnormally with sediment diameter and diminish rapidly in all cases
- For the depth of 1.5 m, MPM gives constant sediment discharge
- Applicable to steep slope of energy grade line to small depth
- Original formula based on the experience of uniform flow in laboratory:
 - -Slope: 1/50 1/2500
 - -Diameter: 0.4 mm 30 mm
 - -Depth: 1 cm<h<1.2m

A & W and E & H

- Abrupt increase of sediment discharge for the fine sand (D<0.2 mm)</p>
- For coarse sand (D>1 mm) with mild slope of energy grade (I<1/7500), it diminish rapidly</p>
- Give an unacceptable sudden variation at a limit of application because of the exponential coefficient, m in the formula
- E&H formula gives the results varying in a good sense for 0.005 mm- 100 mm



(Fig. 11) Exponent, m, used by A & W formula

Van Rijn

- Van Rijn part 1 and II formula generally applicable for the range of 0.1 mm<D<2 mm with a mild slope of energy grade line and deep water
- Careful for using this formula for a small depth and very fine sand
- Van Rijn part III is applicable for the range of 0.005 mm<D<2 mm except for a small depth (h<0.8 mm)</p>
- Need attention for a small depth with a mild slope

Numerical Model - Non-equilibrium Sediment Transport

- Create fully coupled one-dimensional mobile bed model
- Condition of unsteady flow
- Non-equilibrium sediment transport
- With looped network system
- Mobile Cross Section
- 4 Governing equation plus additional equations
 - Continuity Motion
 - Conservation of material in suspension
 - Conservation of bed-material
 - Sediment transport formula
 - Roughness coefficient (considering Bed Form)
 - Pick-up function and Fall velocity

Map of Modeling Boundary

Ceyzerieu Massing Vions Chindrieux Pugieu • Cuzieu Vongnes - Flaxieu Lavours Chanaz Chazey-Bons Pollieu Cessens Marignieu Andert-et-Condon Conjux Saint-Germain-la-Chamb Cressin-Rochefort Magnieu Saint-Champ Saint-Pierre-de-Curtille Belley 01300 Belley, France Massignieu-de-Rives Ontex Lucey Parves Jongieux Nattages Brison-Saint-Innocent Brens Grésv Billième Virignin ©2010 GOO 2010 Tele Atlas © 2010 Google La Balme 2010 IGN-Erance La Chapelle-du-Mont-du-Chat

PLAN D'ENSEMBLE DE L'AMENAGEMENT



Chanez Diversion



Cressin Lake





Map of Belley Reservoir



Map of Belley Reservoir

Cross Section & Velocity Data (CNR)



Continue

C.N.R.	Mesure de vitesses au P 126.950 Le 03-06-1993 (11h30-12h40) Niv moy: 234.16 N.6 c 31 T/T Helice n 95 875		
N: 0003	RESULTATS 0 - 533, M/S 5 - 1685, M2		

Right Bank

Left Bank



Cressin Lake (Confluence & Divergence)



== Bed Elevation

O Ground Elevation (m NGF)



Definition Sketch



Definition Sketch in the Sediment Transport Model

Continue



Governing Equations

Fluid continuity equation:

$$\frac{\partial A}{\partial t} + \frac{\partial Q}{\partial x} = B \frac{\partial z}{\partial t} + \frac{\partial Q}{\partial x} = q \qquad (1)$$

Fluid motion equation:

$$\frac{\partial z}{\partial t} + \frac{1}{gA}\frac{\partial}{\partial x}\left(\beta\frac{Q^2}{A}\right) + \frac{Q^2}{K^2} + \frac{1}{gA}\frac{\partial Q}{\partial t} + \frac{Ke}{2g}\frac{\partial(Q/A)^2}{\partial x} = 0$$
(2)

Suspended material conservation equation:

$$\frac{\partial CA}{\partial t} + \frac{\partial Qs}{\partial x} = S - qC$$
(3)

Bed material conservation equation:

$$(1-p)\frac{\partial Ab}{\partial t} + \frac{\partial Qb}{\partial x} + S = 0$$
(4)

in which x = streamwise coordinate; t = time; A = wetted cross-sectional area; Q = discharge; Z = watersurface elevation above a datum; B = flow width; q = lateral flow; g = gravitational acceleration; β = momentum correction coefficient; K = conveyance; Ke = coefficient of expansion-contraction; C = average sediment concentration; Qs = volumetric suspended load; S = sediment flux between bottom layer and waterstream; Ab = bottom layer cross-section; Qb = bed load.

Discretization of Equation

$$\frac{\partial f}{\partial t} = \frac{1}{\Delta t} \left[\left[\psi \Delta f_{i+1} + (1 - \psi) \Delta f_i \right] \right]$$
$$\frac{\partial f}{\partial x} = \frac{1}{\Delta x} \left[\left(f_{i+1} + \theta \Delta f_{i+1} \right) - \left(f_i + \theta \Delta f_i \right) \right]$$

 $f(\mathbf{x},t) = \psi \left(f_{i+1} + \theta \Delta f_{i+1} \right) + (1-\psi) \left(f_i + \theta \Delta f_i \right)$

which i and n = gird point, θ = the weighting factors for time, ψ = the weighting factors for space

Solution for Algebraic System

 $\Delta Q_i = F_i \Delta Z_i + G_i \Delta Z b_i + H_i \Delta C_i + K_i$ $\Delta C_i = F_j \Delta Z_i + G_j \Delta Z b_i + H_j \Delta Q_i + K_j$ in which F_i, F_j, G_i, G_j, H_i, H_j, K_i and K_j are known coefficients for the given time.

$$\Delta Q_{i+1} = F_{i+1} \Delta Z_{i+1} + G_{i+1} \Delta Z b_{i+1} + H_{i+1} \Delta C_{i+1} + K_{i+1}$$
$$\Delta C_{i+1} = F_{j+1} \Delta Z_{i+1} + G_{j+1} \Delta Z b_{i+1} + H_{j+1} \Delta Q_{i+1} + K_{j+1}$$

Looped Network



For divergence (A12), the following compatibility condition is used: (FIG.)

$$Z_A = Z_1 = Z_2$$
, $Zb_A = Zb_1 = Zb_2$, $C_A = C_1 = C_2$, $Q_A = Q_1 + Q_2$

For confluence (B34), the following compatibility condition is used:

$$Z_B = Z_3 = Z_4$$
, $Zb_B = Zb_3 = Zb_4$, $C_3Q_3 + C_4Q_4 = C_BQ_B$, $Q_B = Q_3 + Q_4$

Application to River

The size distribution for bed material and suspended load are:

Bed material: $D_{16} = 0.034 \text{ mm}$, $D_{50} = 0.150 \text{ mm}$, $D_{84} = 0.288 \text{ mm}$, $D_{90} = 0.375 \text{ mm}$ Suspended load: $D_{16} = 3.4 \mu \text{m}$, $D_{50} = 11.5 \mu \text{m}$, $D_{84} = 28.0 \mu \text{m}$, $D_{90} = 36.0 \mu \text{m}$

Using $\Delta t = 5$ minute and D = 11.5 µm for the condition of Q = 700 m³/s, Z = 233.93 m, Zb = 255 m and varying C, the concentration variation along the Belley reservoir shows as follows: (FIG. 5)

The flushing operation in 1990 is lasted about 4 days. The discharge during 4 days changes with minimum Q = 512 m³/s and maximum Q = 990 m³/s. During flushing the concentration variation is observed with minimum C = 0.7 g/l and maximum C = 9 g/l. The concentration variation for 5 μ m, 11.5 μ m, 20 μ m, and 30 μ m are also given in the following figure. (FIG.6)



PK

Water Surface Profile (Q = 715 m3/s, Z = 233.93 m, Zb = 225 m; May 25, 1990)





Discharge at Upstream Boundary

Variation of concentration at Upstream (Vions)



Concentration Variations at Downstream Depending on Sediment Diameter



Trap Efficiency

TABLE 1. Trap Efficiency of Sediment

Diameter(µm)	Inflow(m ³)	Deposit(m ³)	Outflow(m ³)	Trap(%)
5.0	295,000	3,000	292,000	1
11.5	295,000	84,000	211,000	28
20.0	295,000	201,000	94,000	68
30.0	295,000	284,000	31,000	89

Results

- □ D=5 µm almost transported to downstream
- D=30 µm almost deposited in reservoir
- Sediment inflow 295,000 m³
- **D** Suppose:
 - D=5 µm (30%) very fine silt
 - D=11.5 µm (30%) fine silt
 - D=20 µm (20%) medium silt
 - D=30 µm (20%) coarse & medium silt
- Trap efficiency=Deposit/inflow=119,000/295,000 = 40% = 0.4

Continue

- D=5 µm pass through the reservoir
- D=30 µm 89% deposited in the reservoir
- Trap efficiency of model simulation (=0.4) gives reasonably good result comparing the measurement (=0.49) in 1990

O'Conner Lakes of Feather River (Q= 65,000 cfs, Jan. 4, 2006)



O'Conner Lakes of Feather River (Q= 65,000 cfs, Jan. 4, 2006) > 210,000 cfs (100yr)



Debris/Sediment Trap after Flooding



Sediment Deposit after removing Debris (Q= 65,000 cfs, Jan. 4, 2006 at O'Conner Lakes, Feather River)



Feather River Sediment Deposit



Next Step

- Apply to channels and natural rivers system (Sacramento River, Feather River & San Joaquin River)
- Combined with GIS and Water Quality Model
- Combined with 2-D hydraulic model
- Long term maintenance, Channel capacity study, Project planning
- Need to consider the change of bed elevation due to major flood events with mobile bed model
- Consider cumulative impact of sediment deposit and erosion

Environmental restoration

- carefully designed or planned for heavy sediment carrying/ transporting stream
HEC-RAS Sediment Model – unsteady version of sediment transport: not available

Chapter 17 Performing a Sediment Transport Analysis

CHAPTER 17 Performing a Sediment Transport Analysis

This chapter shows how to perform a mobile bed sediment transport analysis with HEC-RAS. A sediment model requires a geometry file, a quasi-unsteady flow file, a sediment file and a sediment analysis plan file. Instructions on creating a geometry file can be found in Chapter 6 of this User's Manual. The other three files are described in this chapter.

P17-1

Transport Function

A transport function can be selected from the drop down box near the top of the form. There are currently seven transport functions to select from:

Ackers and White

Englund • England and Hansen

- Copeland's form of Laursen
- Meyer, Peter and Muller
- Toffaleti
- Yang (sand and gravel eqns.)
- Wilcock

Fall Velocity Methods

Several methods are available for computing fall velocity and the user should select the most appropriate algorithm. The options include:

- Ruby
- Toffaleti
- Van Rijn
- Report 12 (Default method in HEC-6)

p17-3

p17-2

Q & A

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Sediment Transport Modeling

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Vegetation Issues & Roughness Coefficient







Development of Integrated Water Quality Management System of Watershed -GIS and Water Quality Model-



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Sept, 2009.